

$$\vec{r}(x, y, z), \quad \vec{A}(a, b, c), \quad a, b, c = \text{const.}$$

$$\vec{r}^2 = x^2 + y^2 + z^2$$

$$\vec{r}^2 \vec{A} = (a(x^2 + y^2 + z^2), b(x^2 + y^2 + z^2), c(x^2 + y^2 + z^2))$$

$$\text{Div}(\vec{r}^2 \vec{A}) = \left(\frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z} \right) \cdot (\vec{r}^2 \vec{A})$$

$$= \frac{\partial(a(x^2+y^2+z^2))}{\partial x} + \frac{\partial(b(x^2+y^2+z^2))}{\partial y} + \frac{\partial(c(x^2+y^2+z^2))}{\partial z} = 2ax + 2by + 2cz = 2(\vec{r} \cdot \vec{A})$$

$$\vec{r} \times \vec{A} = (cy - bz, az - cx, bx - ay)$$

$$\text{Rot}(\vec{r} \times \vec{A}) = \left(\frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z} \right) \times (\vec{r} \times \vec{A})$$

$$= \left(\frac{\partial}{\partial y}(bx - ay) - \frac{\partial}{\partial z}(az - cx), \frac{\partial}{\partial z}(cy - bz) - \frac{\partial}{\partial x}(bx - ay), \frac{\partial}{\partial x}(az - cx) - \frac{\partial}{\partial y}(cy - bz) \right)$$

$$= (-2a, -2b, -2c) = -2\vec{A}$$